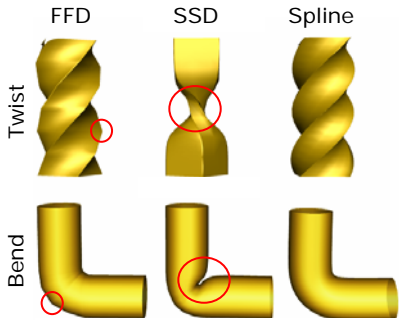


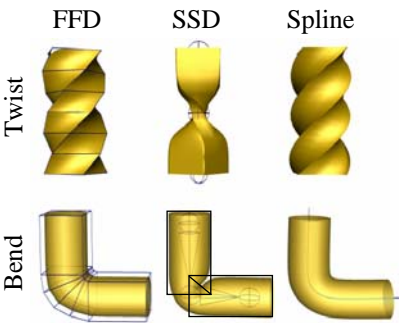
Fast Skeletal Animation by skinned Arc-Spline based Deformation

Sven Forstmann and Jun Ohya

Deformation Types



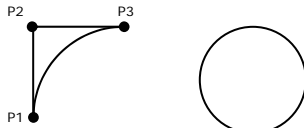
Detailed



Lattice based Free Form Deformation Skeletal Subspace Deformation Spline aligned deformation Wires 'SIG98

Spline Functions

Arc-Spline



- Seamless round
- Fast to evaluate
- Numerically stable

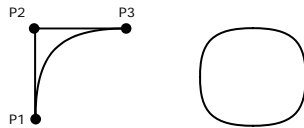
$$\forall x \in [0, \pi/2]$$

$$f_a(x) = P1 + \frac{P1P2 \cdot \sin(x)}{P1P2 \cdot \cos(x) + P2P3} + \frac{P2P3 \cdot (1 - \cos(x))}{P1P2 \cdot \cos(x) + P2P3}$$

$$f_a'(x) = \frac{P1P2 \cdot \cos(x)}{P1P2 \cdot \cos(x) + P2P3} - \frac{P2P3 \cdot \sin(x)}{P1P2 \cdot \cos(x) + P2P3}$$

10 arithmetic operations total

Bézier-Spline



- Not seamless round shaped
- Slow evaluation

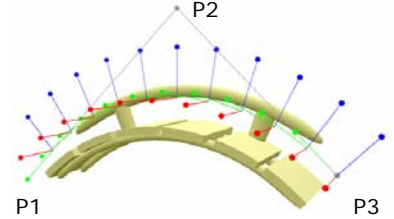
$$\forall x \in [0, 1]$$

$$f_b(x) = P1 \cdot (1-x)^2 + P2 \cdot 2 \cdot x \cdot (1-x) + P3 \cdot x^2$$

$$f_b'(x) = P1 \cdot 2 \cdot (x-1) + P2 \cdot 2 \cdot (1-2 \cdot x) + P3 \cdot 2 \cdot x$$

19 arithmetic operations total

Coordinate System



The TNB Frenet Frame

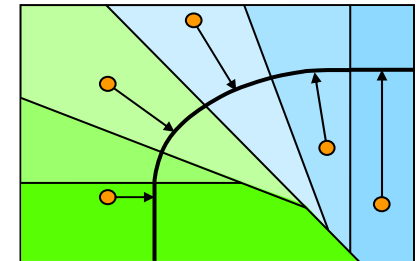
Origin : $b_o(x) = f_a(x)$

Tangent : $b_T(x) = f_a'(x)$

Normal : $b_N = P1P2 \times P2P3$

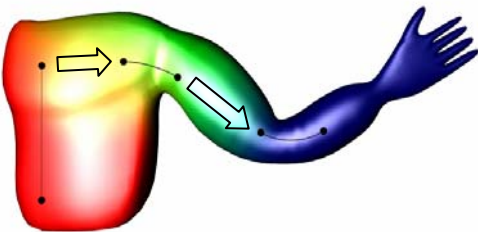
Binormal : $b_B(x) = b_T(x) \times b_N$

Spline Binding



● Vertex — Spline — Bind partition

Weighted Spline Mixing



Rigid "ghost" skeleton

Body spline S_1

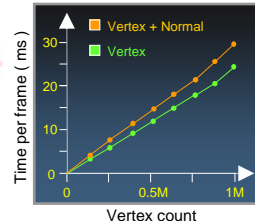
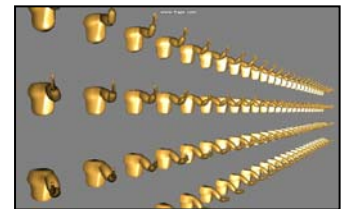
Arm spline S_2

Elbow spline S_3

$$1 = \sum_{i=1}^3 w_i$$

$$v = \sum_{i=1}^3 S_i \cdot w_i$$

Results from Real-Time Spline Deformation



1M Vertices @ 43 fps

= 1000 Characters with 1000 Vertices each animated at 43 fps !

Hardware: Pentium IV 3.2 Ghz Nvidia GeForce 7800 GTX